



# Image Analysis

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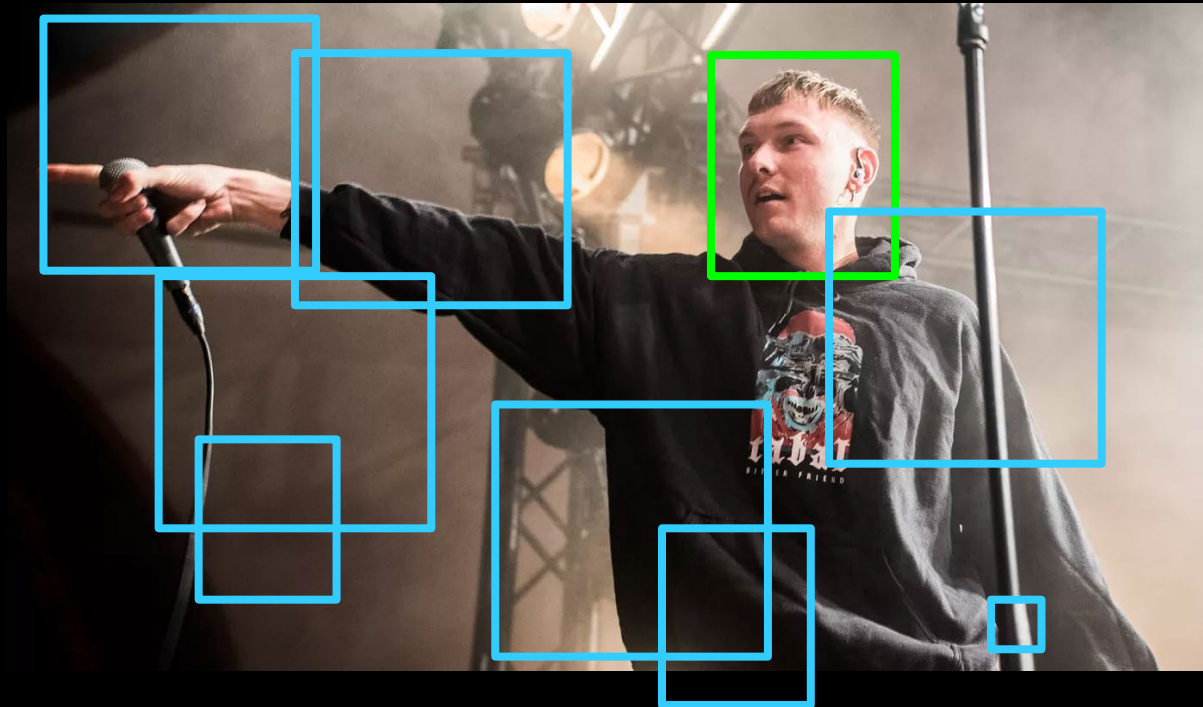
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<http://www.compute.dtu.dk/courses/02502>

# Lecture 11 – Face detection using the Viola Jones method

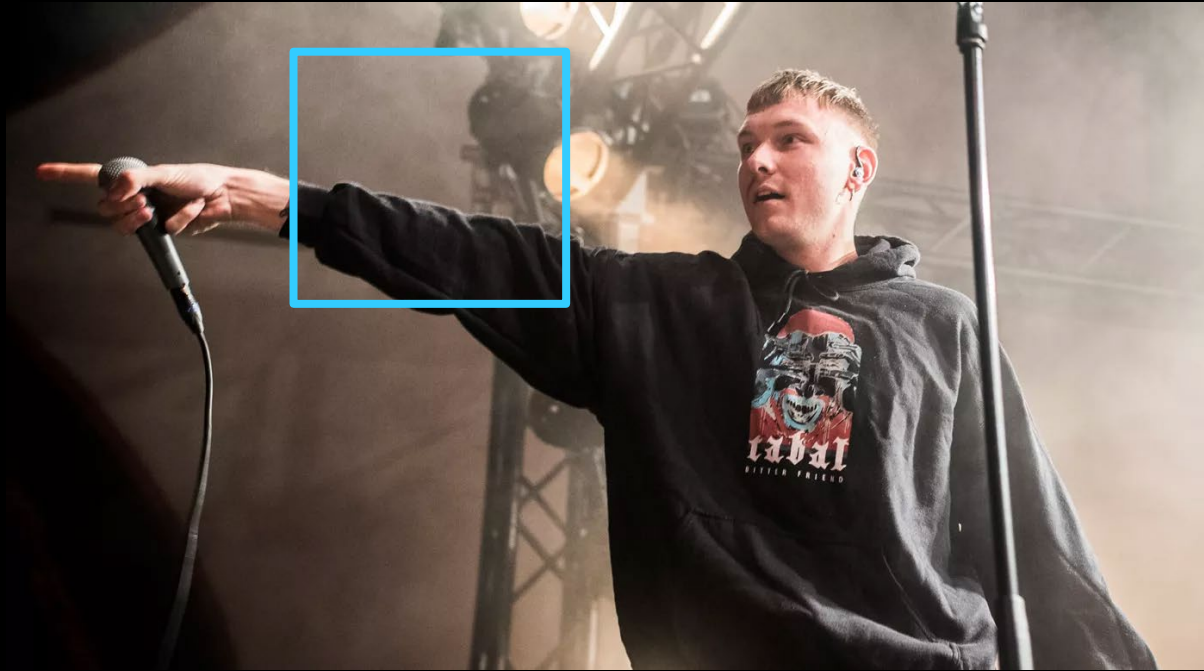




## What can you do after today?

- Describe the concept of face detection
- Describe the concept of Haar features
- Compute the values of 2, 3 and 4 rectangle Haar features
- Describe the integral image
- Compute the sum of pixels values in a rectangle using an integral image
- Describe the concept of a weak classifier
- Describe how several weak classifiers can be combined into a strong classifier
- Describe the attentional cascade
- Describe how faces can be detected using a moving window

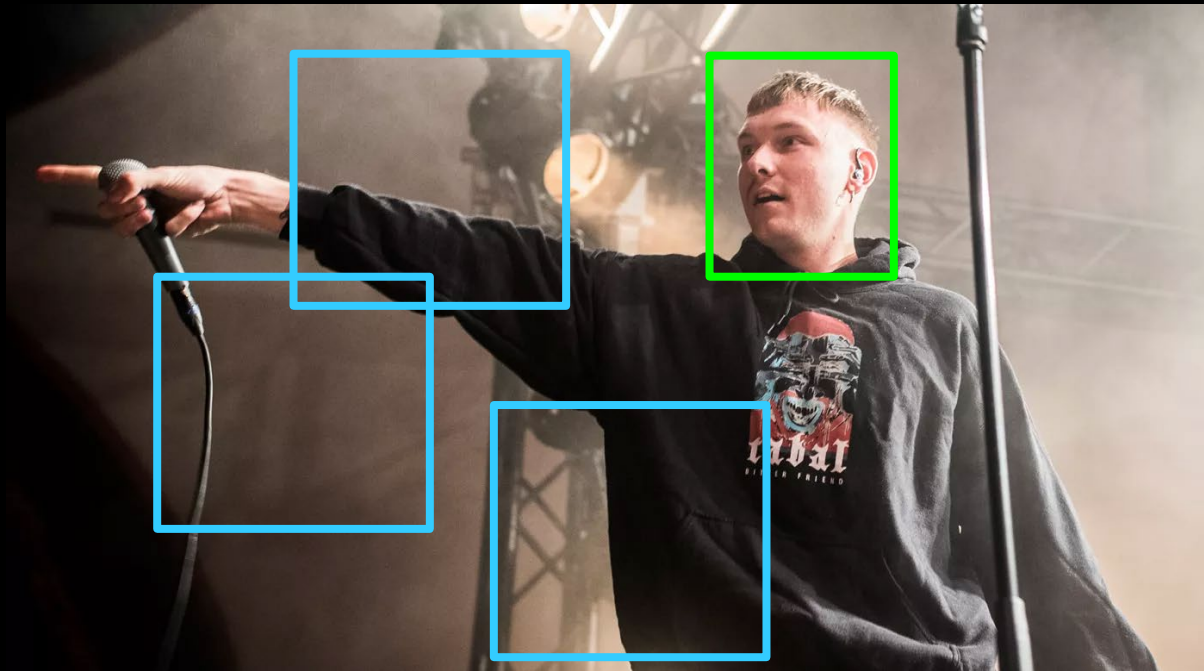
# Face detection



## ■ First problem

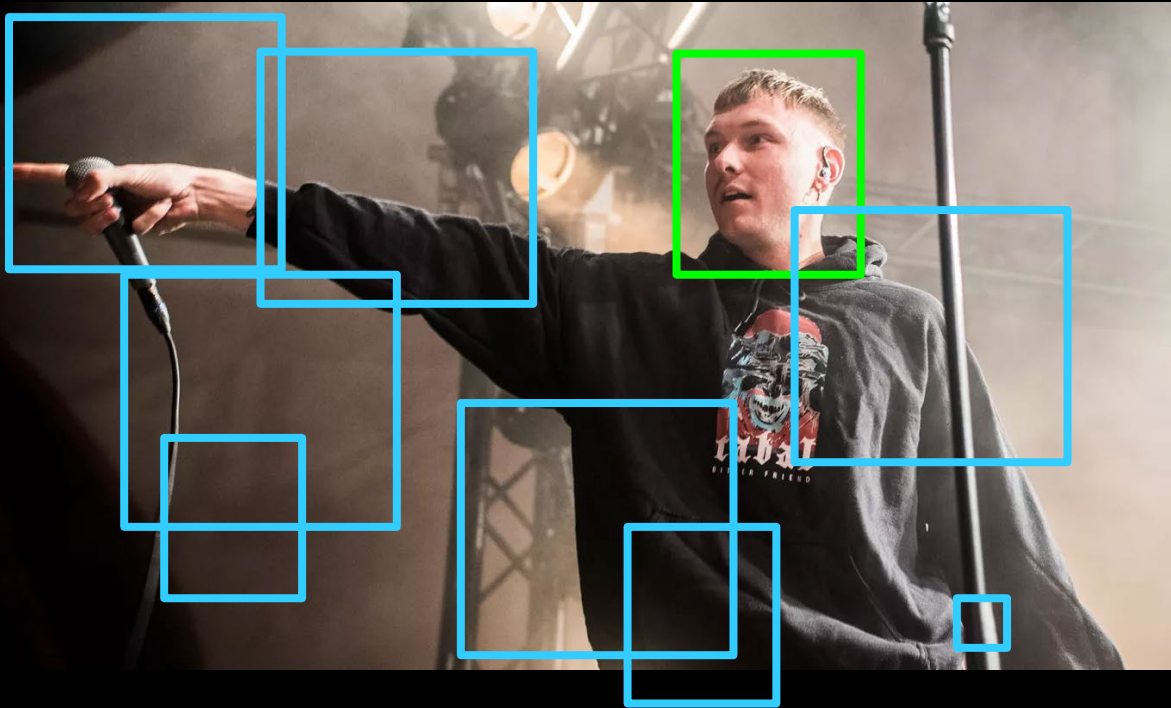
- Analyze a **window** in an image
- Is there a face in that window?

# Face detection



- Slightly more advanced
  - Analyze many **windows** in an image
  - How many (if any) **windows** contain faces?

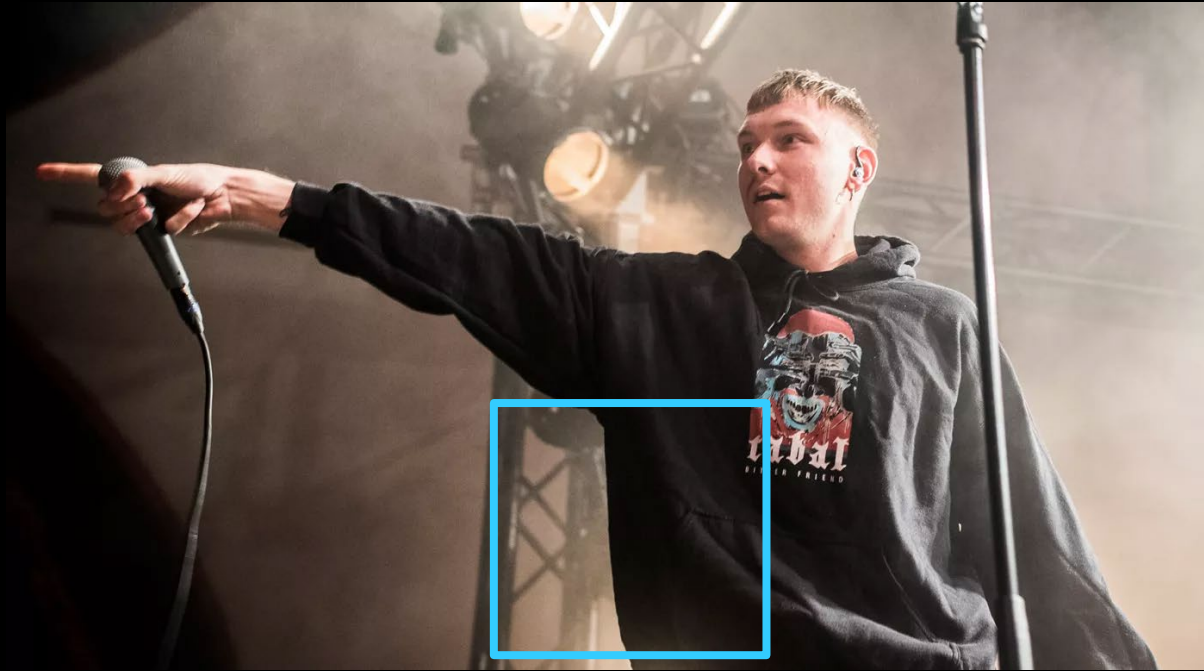
# Face detection



## ■ Ideal

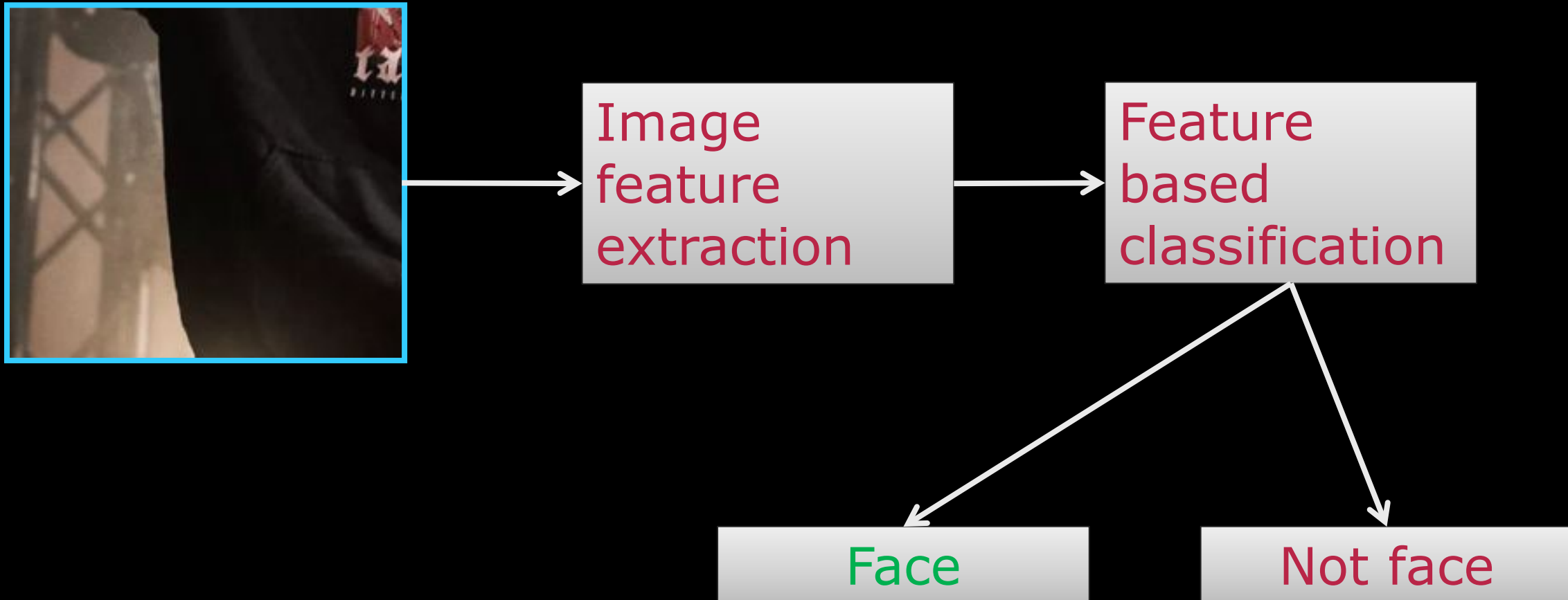
- Analyze (almost) all possible **windows** in an image
- How many (if any) **windows** contain faces?

## What is needed?



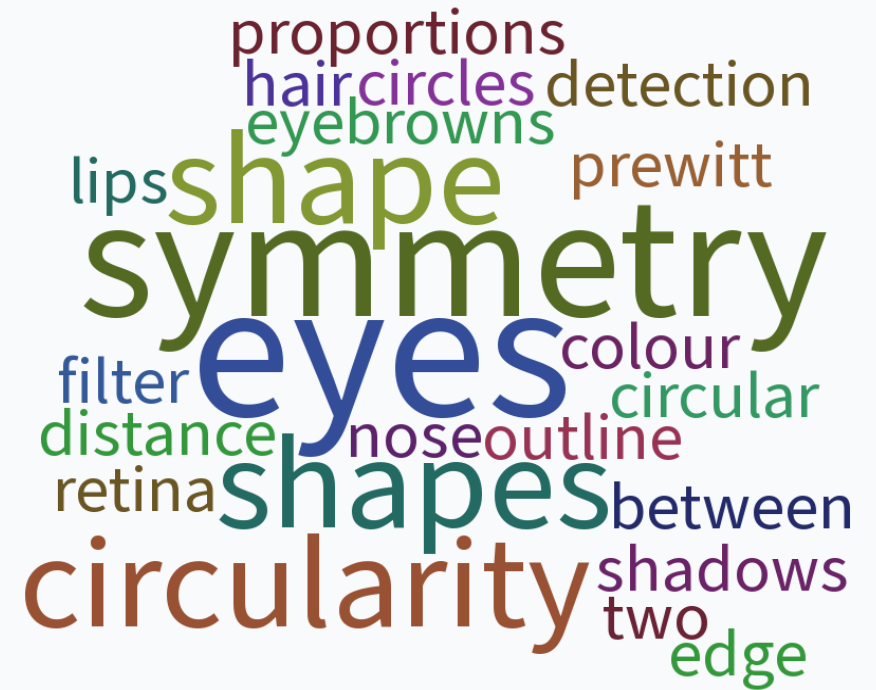
- A fast method to determine if a *window* contains a face

# Primary task – image feature based classification





### Image based features - what features can you think of?



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# Viola Jones – fast features and smart classification



Many image  
features  
very fast

Boosted  
cascade  
classifier

Face

Not face



# Training data



## ■ Face images:

- 4916 hand labelled faces
- Aligned and scaled to 24x24 pixels

## ■ Non-face images:

- 9544 images with no faces
- 350 million sub-windows sampled from these

# Viola Jones – fast features and smart classification



Many image  
features  
very fast

Boosted  
cascade  
classifier

Face

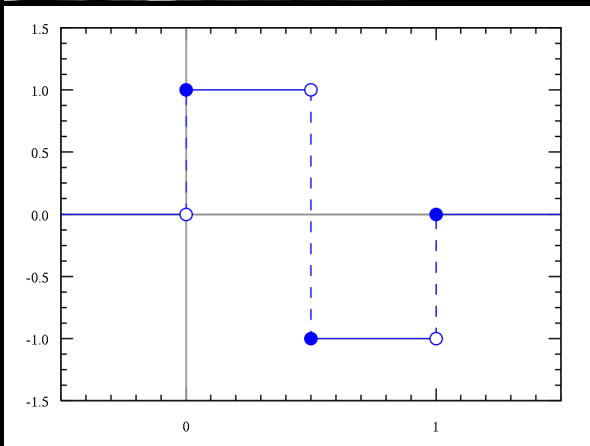
Not face

# Haar features



- Alfred Haar (1885-1933)
  - Hungarian Mathematician
- Introduced the Haar wavelet in 1909
- *A wavelet is a wave-like oscillation with an amplitude that begins at zero, increases or decreases, and then returns to zero one or more times.*
- Simplest possible wavelet

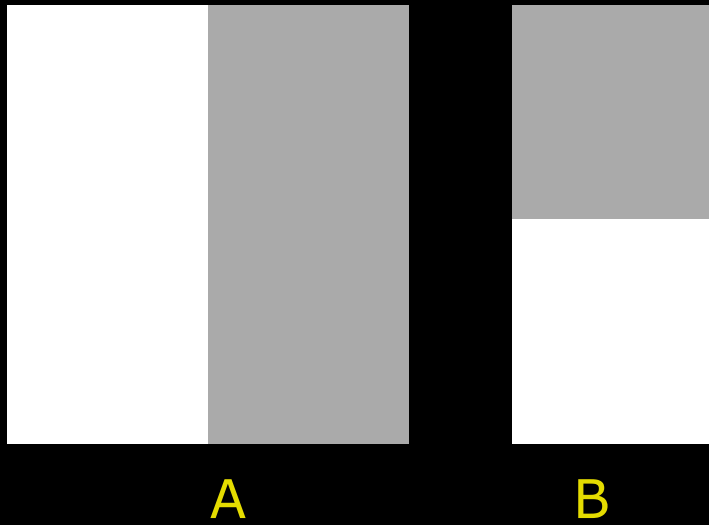
<https://en.wikipedia.org/wiki/Wavelet>



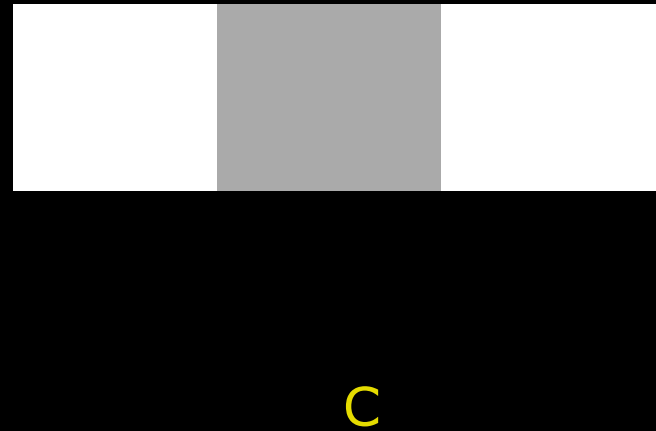
[https://en.wikipedia.org/wiki/Haar\\_wavelet](https://en.wikipedia.org/wiki/Haar_wavelet)

# Haar features

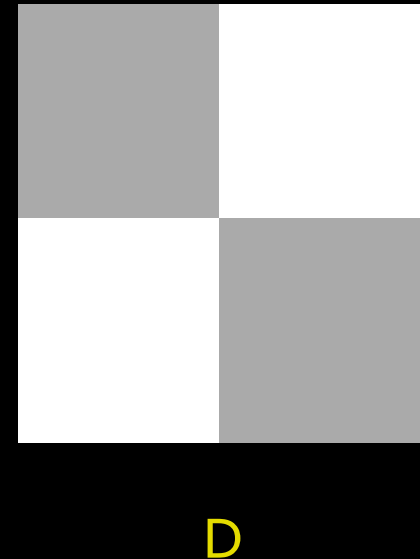
Two rectangle features



Three rectangle feature



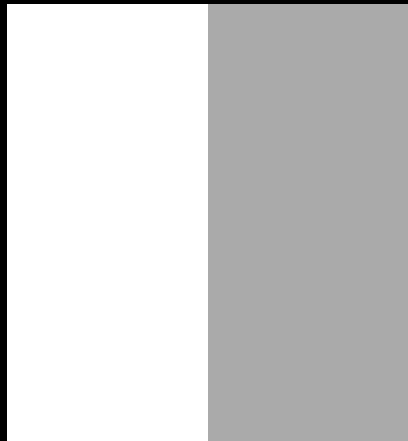
Four rectangle feature



$$\text{Feature} = \begin{matrix} \text{Sum of} \\ \text{pixel} \\ \text{values} \\ \text{in image} \end{matrix} - \begin{matrix} \text{Sum of} \\ \text{pixel} \\ \text{values} \\ \text{in image} \end{matrix}$$



# One Haar feature



A

3	42	115	137	1	66
86	154	21	254	198	204
41	67	58	20	208	110
203	167	233	113	222	232
79	176	39	27	22	46
135	191	211	245	102	67

$$\text{Feature} = 254 + 198 + 20 + 208 + 113 + 222 - 154 - 21 - 67 - 58 - 167 - 233 = 1015 - 700 = 315$$



### Four rectangle Haar feature - what is the feature value?

567

179

-611

-113

76

I do not know

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### Four rectangle Haar feature - what is the feature value?



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### Four rectangle Haar feature - what is the feature value?



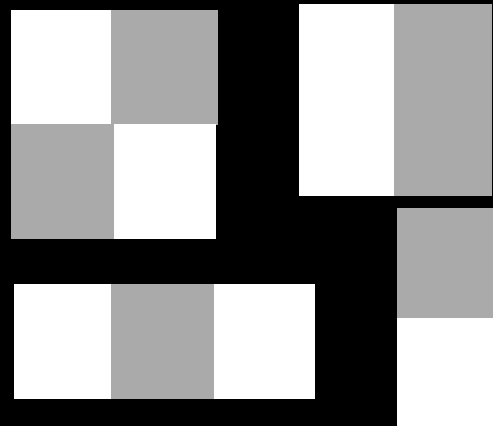
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## Fast computing of Haar features

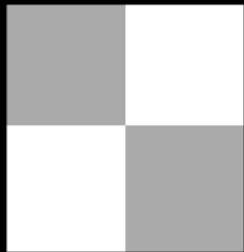


24 x 24 pixels



- Even for small Haar features, there are quite a lot of basic operations
- The larger the Haar feature, the more operations
- We need a fast way to compute Haar features

How many basic operations (plus and minus) are needed to compute the feature?

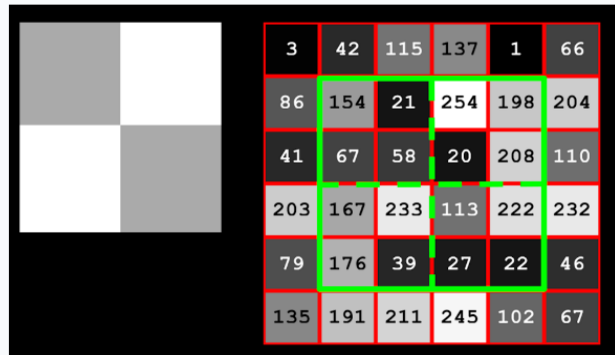


3	42	115	137	1	66
86	154	21	254	198	204
41	67	58	20	208	110
203	167	233	113	222	232
79	176	39	27	22	46
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How many basic operations (plus and minus) are needed to compute the feature?

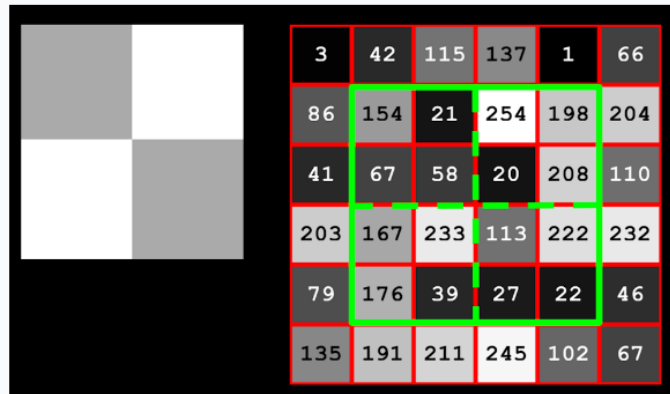


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How many basic operations (plus and minus) are needed to compute the feature?



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# Fast computation of Haar features – the integral image



- In an integral image the pixel value is:
  - The sum of pixel above it and to the left of it in the original image
  - Including the pixel itself
- Can be computed very fast



Computing the integral image - what is the value in the marked pixel?



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### Computing the integral image - what is the value in the marked pixel?

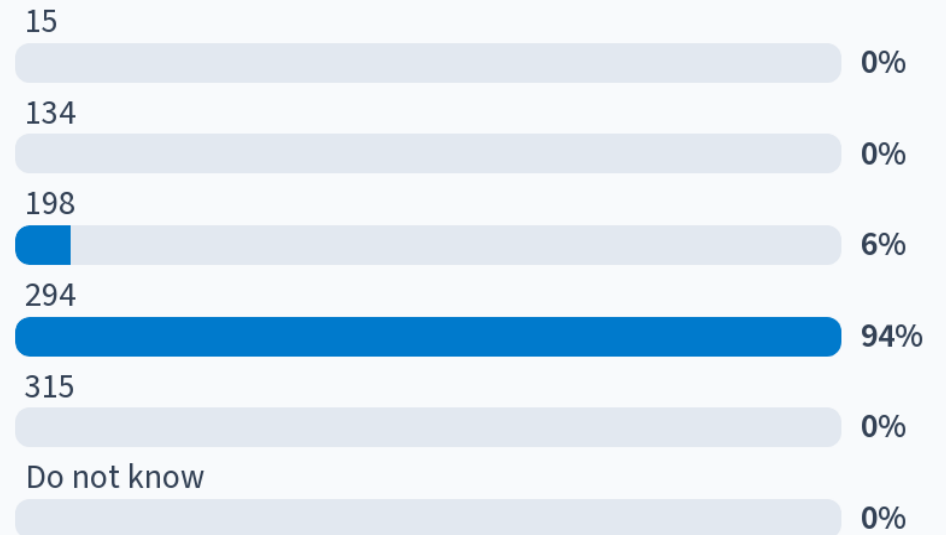


Start the presentation to see live content. For screen share software, share the entire screen. Get help at [pollev.com/app](https://pollev.com/app)



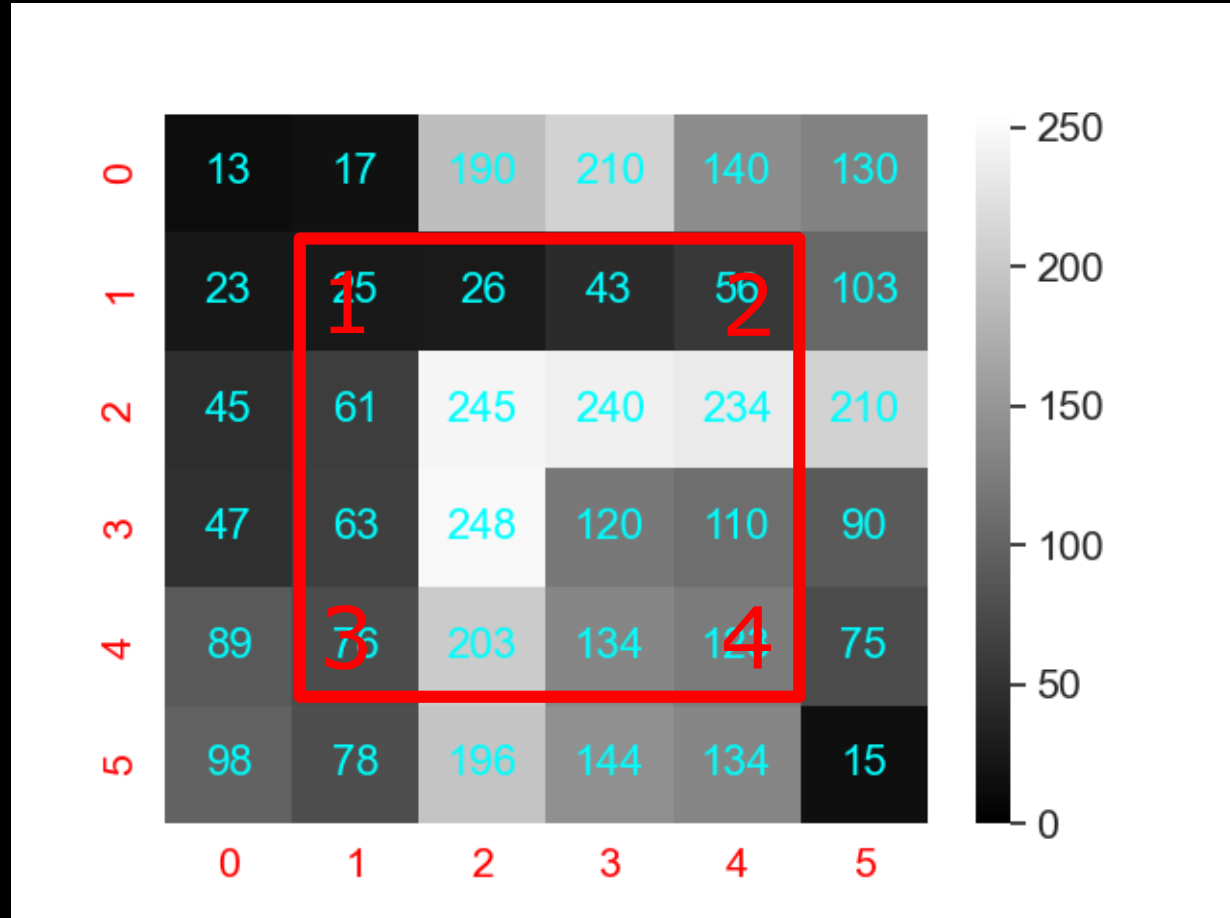


## Computing the integral image - what is the value in the marked pixel?



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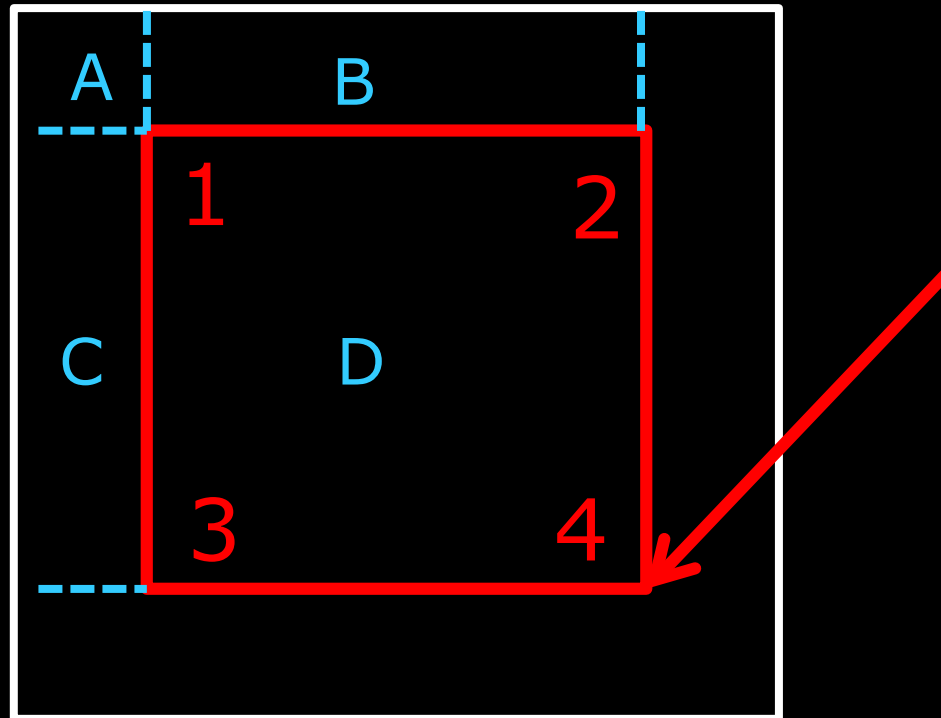
## Using the integral image



- We want to compute the pixel sum in the rectangle
- Defined by four corners: 1, 2, 3, 4



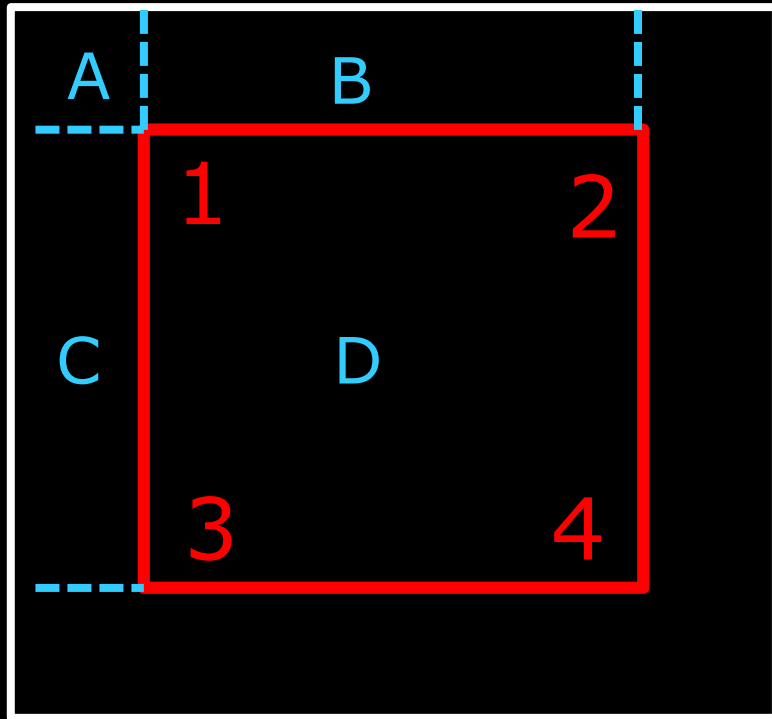
# Using the integral image



- Define four regions:
  - A, B, C, D
- The sum of pixels in the area
  - $A+B+C+D$  is the value of the integral image at point 4



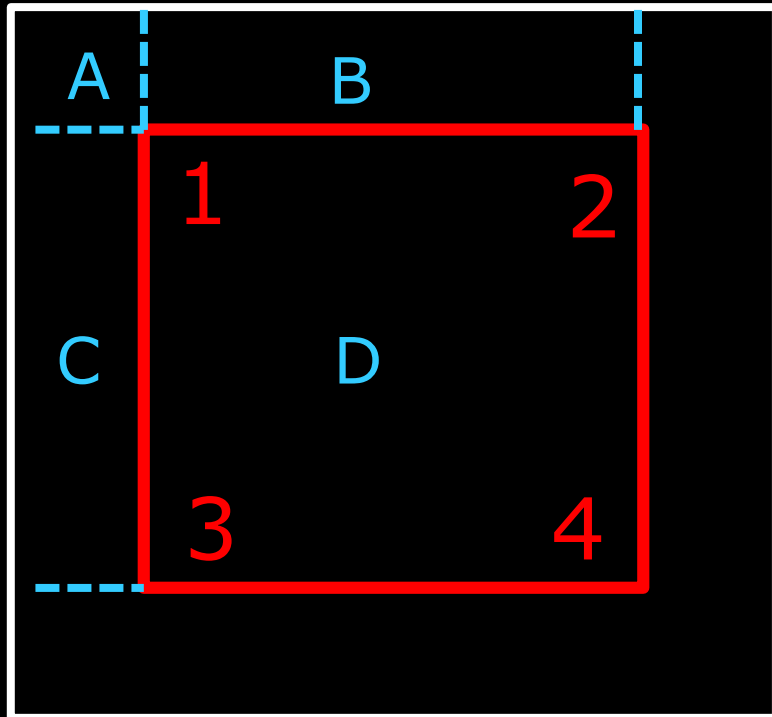
## Using the integral image



- The sum of pixels in the area
  - $A+B$  is the value of the integral image at point 2
  - $A+C$  is the value of the integral image at point 3



## Using the integral image – short notation



### ■ The sum of pixels in the area

$$- \text{ii}(2) = A+B$$

$$- \text{ii}(3) = A+C$$

$$- \text{ii}(4) = A+B+C+D$$

$$- \text{ii}(1) = A$$

$$- \text{ii}(4) - \text{ii}(3) - \text{ii}(2) = D - A$$

### ■ $\text{ii}(4) - \text{ii}(3) - \text{ii}(2) + \text{ii}(1) = D$



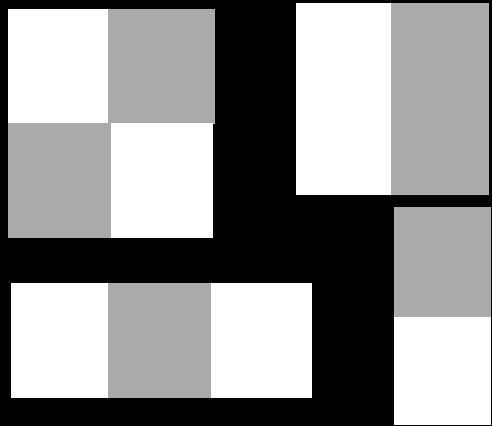
## Course evaluation

- Very important to get your feedback on the course
- Please do it now – log into DTU Inside and fill in the evaluation
- What works well – so we should keep it and strengthen that part
- What can be improved and how?
- The question about “The teacher gave me feedback on my progress”
  - Very hard with large courses
  - We try with quizzes, TAs, exercise solutions

## Haar features in an image window



24 x 24 pixels

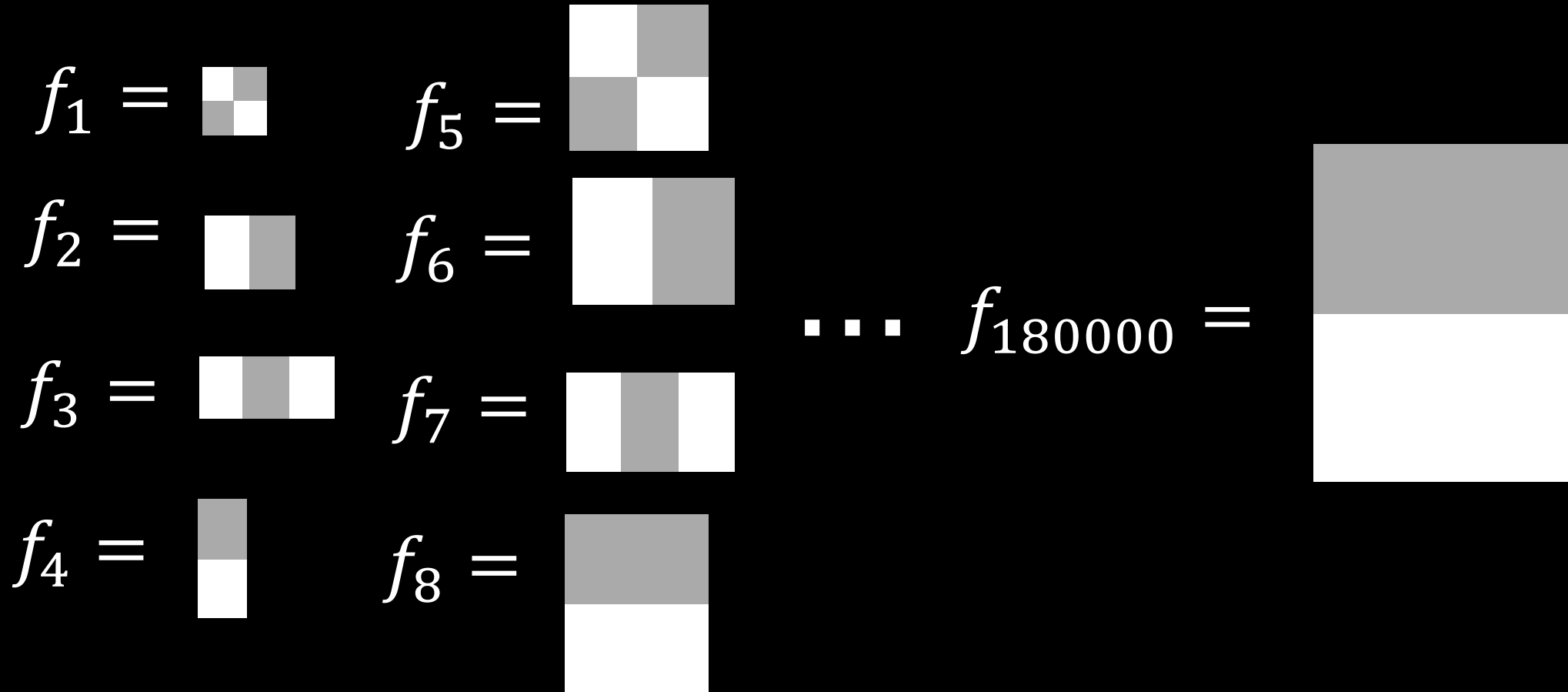


- Image window of 24 x 24 pixels
- All possible sizes and shapes of Haar features
- More than 180.000 features according to Viola and Jones
- They are *overcomplete* – meaning there is a very high redundancy
- We need *feature selection*





## Possible features





# Feature selection – from the article



- There are over 180,000 rectangle features associated with each image sub-window, a number far larger than the number of pixels.
- Even though each feature can be computed very efficiently, computing the complete set is prohibitively expensive.
- Our hypothesis, which is borne out by experiment, is that a very small number of these features can be combined to form an effective classifier.
- The main challenge is to find these features



# Learning Classification Functions

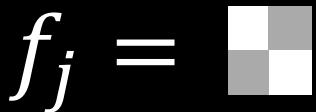


# Weak classifier

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$



24 x 24 sub-window



Feature value computed on the sub-window

$p_j \in [-1, 1]$

Parity – determines if the feature value should be positive or negative

$\theta_j$

Feature threshold



## Weak classifier

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$

$$x = \text{[Image of a person's arm]} \quad f_j(\text{[Small crop of image]}) = \text{[2x2 grayscale grid]} = 2049$$

$$\text{Learnt by training: } p_j = 1 \quad \theta_j = 456$$

$$\rightarrow 1 * 2049 < 1 * 456 \rightarrow h_j(\text{[Small crop of image]}) = 0$$



# What is this parity?



## Weak classifier

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$

$$x = \text{[Image of a person's arm]} \quad f_j(\text{[Crop of image]}) = \text{[2x2 Grayscale Patch]} = 2049$$

Learnt by training:  $p_j = -1$   $\theta_j = 456$

$$\rightarrow -1 * 2049 < -1 * 456 \rightarrow h_j(\text{[Crop of image]}) = 1$$

# Creating a strong classifier from weak classifiers

$$h(x) = \begin{cases} 1 & \sum_{t=1}^T \alpha_t h_t(x) \geq \frac{1}{2} \sum_{t=1}^T \alpha_t \\ 0 & \text{otherwise} \end{cases}$$

$$h_1(\text{img}) = \text{img}$$

$$h_2(\text{img}) = \text{img}$$

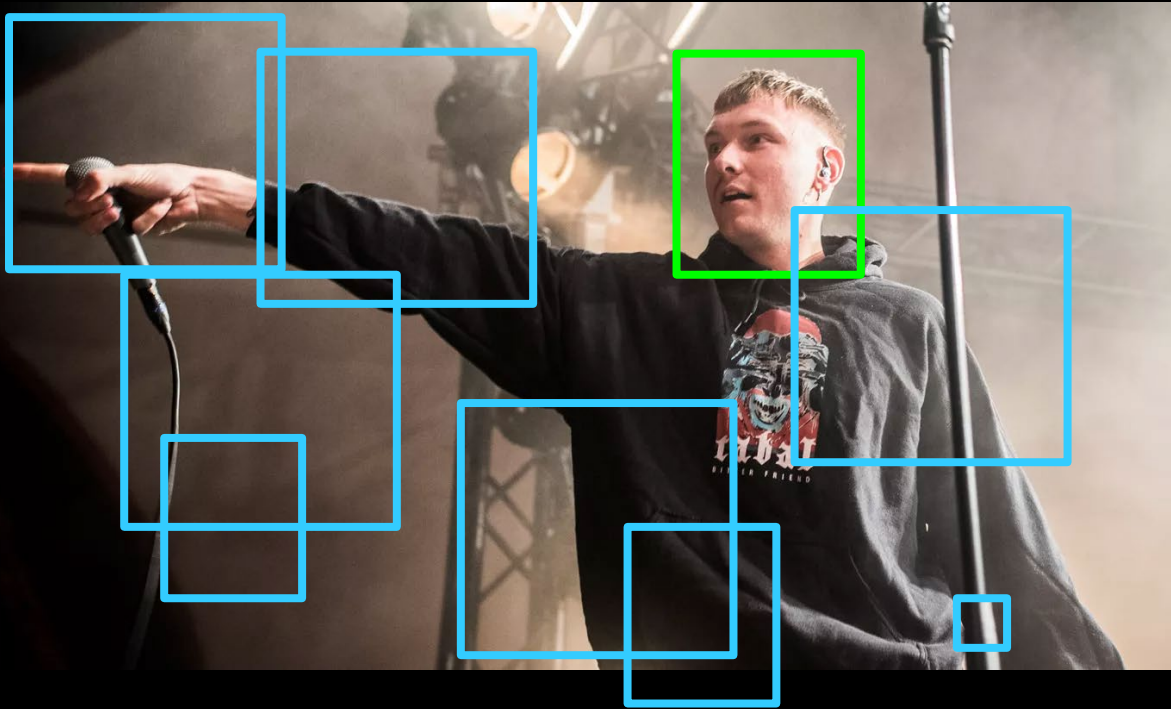
...

$$h(\text{img}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost



## Boosted features – good performance but not enough



- Frontal face classifier with
  - T=200 features
  - Detection rate 95%
  - False positives 1 in 14084
  - 0.7 seconds for a 384 x 288

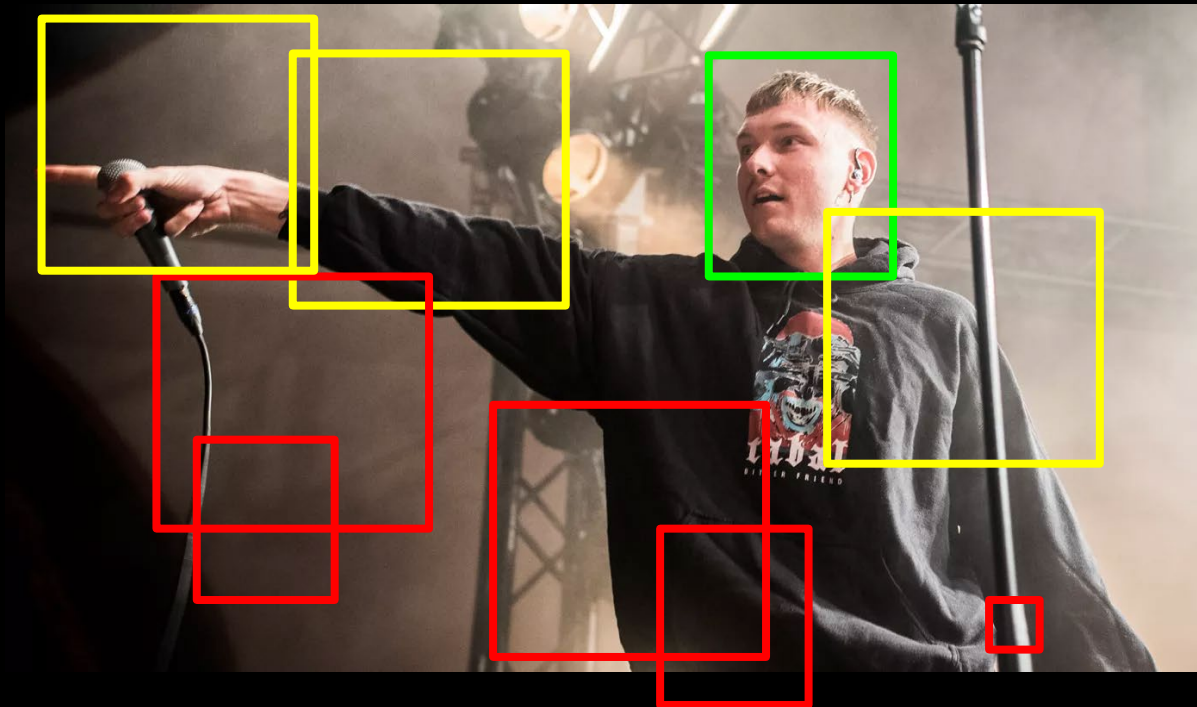
$$h_1(\text{[face]}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

# The Attentional Cascade



# Image Attention

- The process of focusing on specific parts of an image
  - Followed by fine grained analysis of selected windows

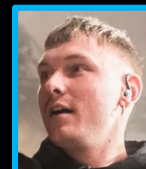
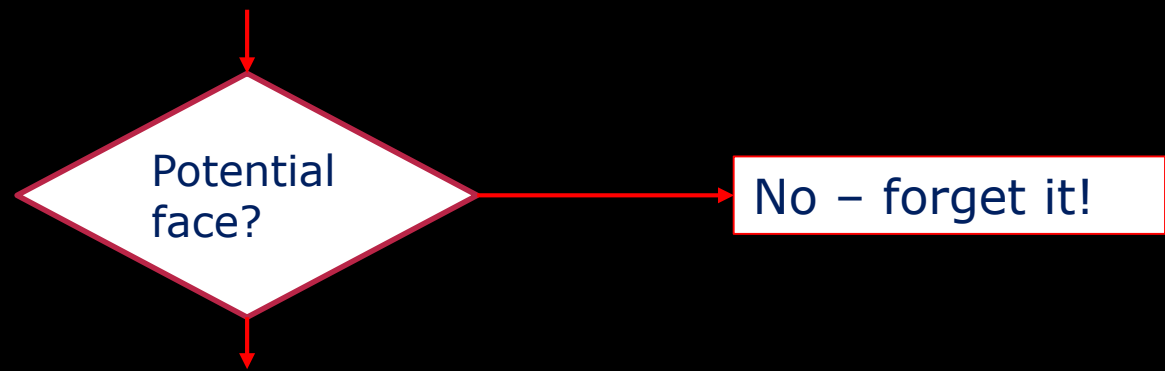
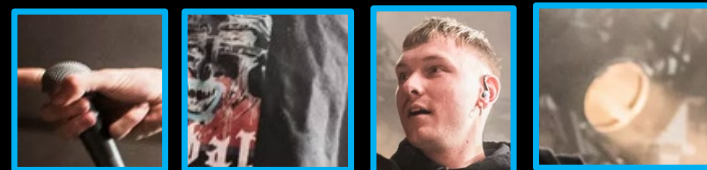
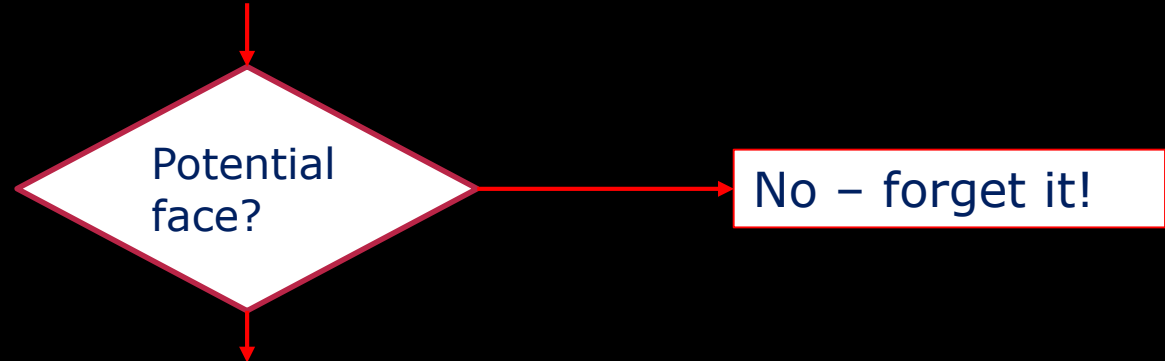


Focusing on potential face regions





# Cascaded classifier



Also called a *degenerate decision tree*



## What is a false negative?

A face window classified as face window

A background window classified as a face window

A face window classified as a background window

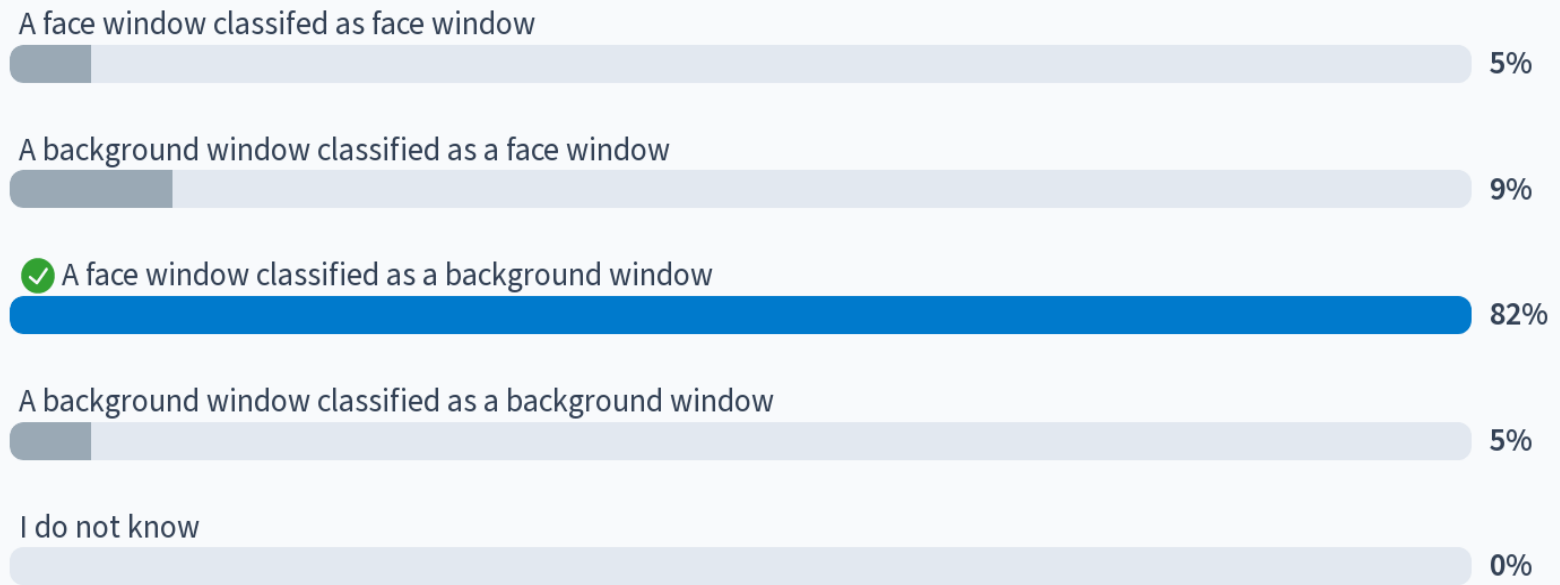
A background window classified as a background window

I do not know

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## What is a false negative?



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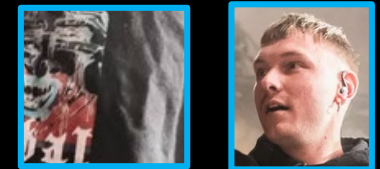
# The attentional cascade



- Quickly reject negative sub-windows
  - Detect almost all positive sub-windows
  - False-negatives close to zero
    - Keep all potential face windows
  - Using the training set to find weights that fulfils this criterion



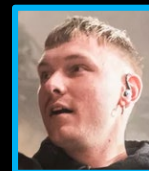
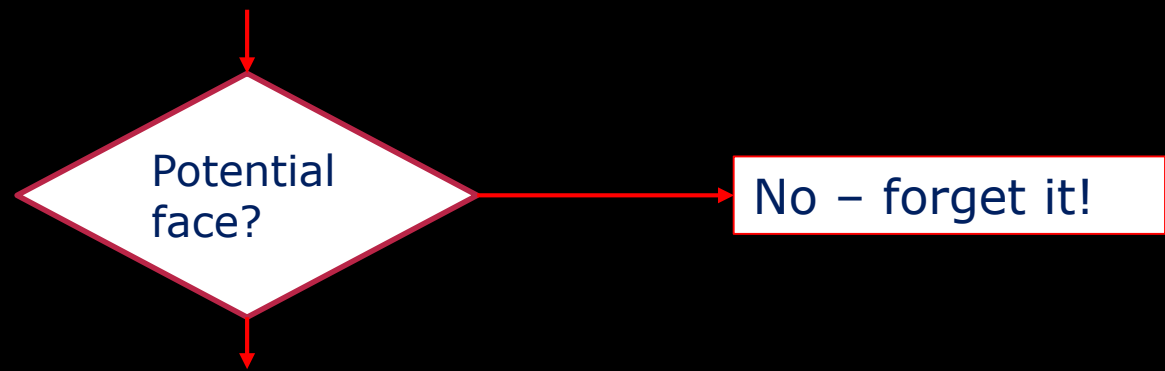
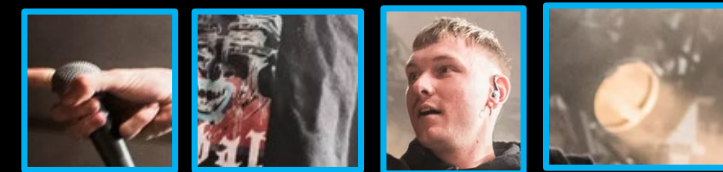
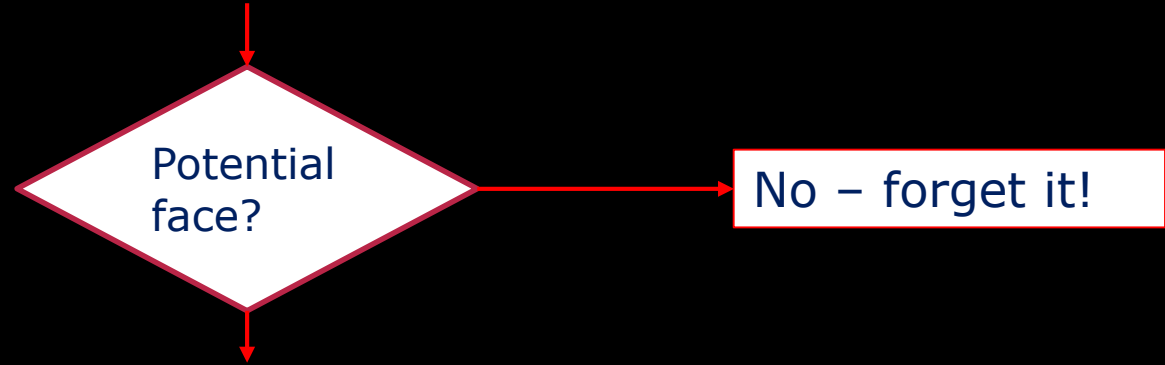
- Later more complex classifier
  - Low false positive rate







# Training a cascade



$$h(\text{img}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost

$$h(\text{img}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost



# First stage classifier

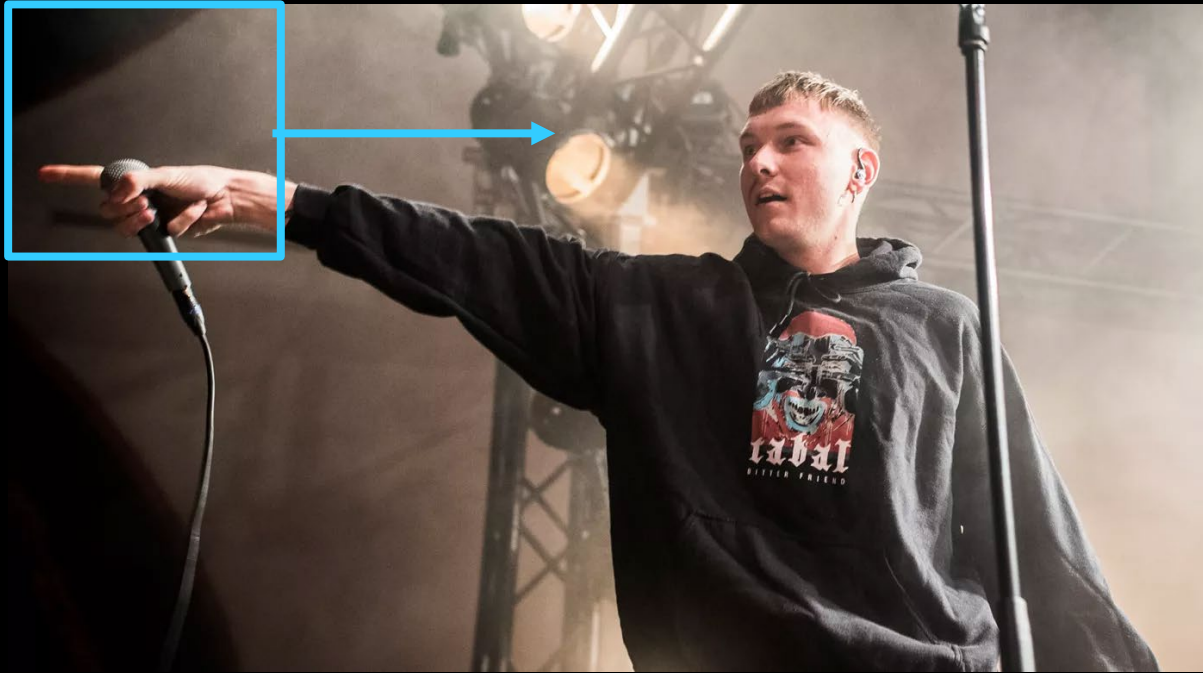


## Final classifier



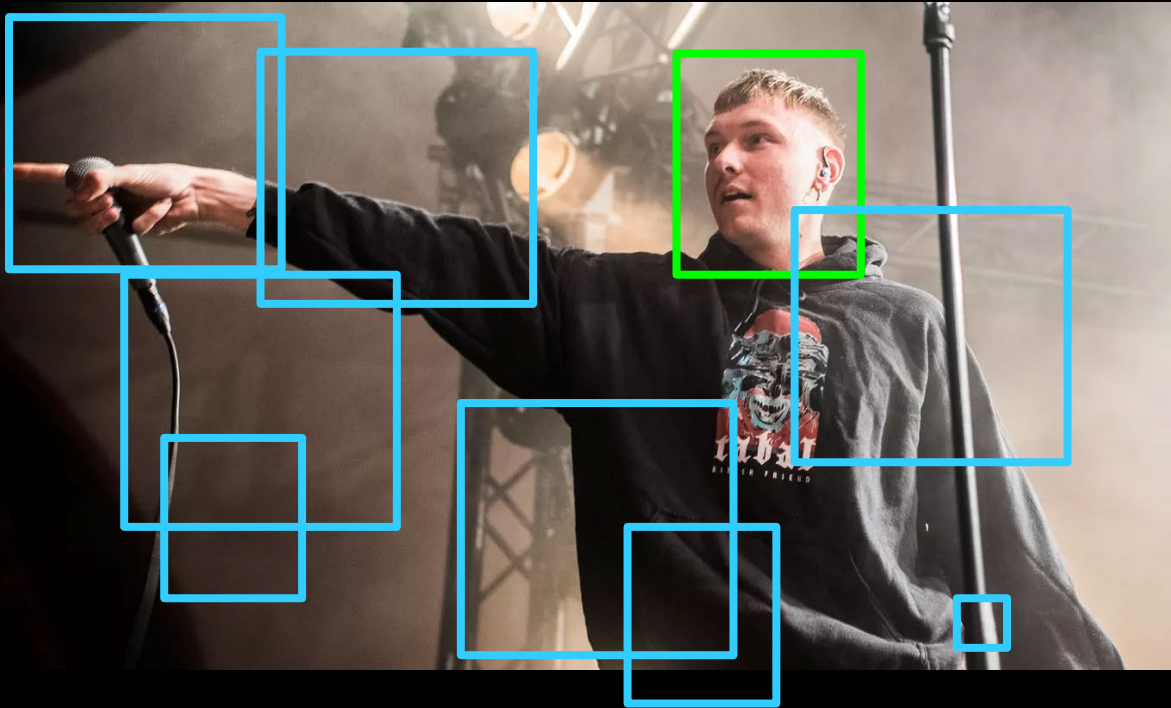
- 38 stages (step in the cascade)
- Total 6000 features (over the entire cascade)
- Faces are detected using on average 10 features per sub-window

## Finding all faces in an image



- Slide a sub-window over the entire image
- Do a face detection for all positions
- Scale the features in a certain interval
  - To find faces of different sizes

# Conclusion



- One of the most important algorithms before deep learning
- Uses many interesting concepts
  - Attention
  - Boosted weak classifiers
  - Very fast feature computation



# Demo





## Next week(s)

- Advanced topics
- Statistical models of shape and appearance